Sharp inequalities for the coefficients of concave schlicht functions

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Abstract

Let D denote the open unit disc and let $f: D \to \mathbb{C}$ be holomorphic and injective in D. We further assume that f(D) is unbounded and $\mathbb{C} \setminus f(D)$ is a convex domain. In this article, we consider the Taylor coefficients a n(f) of the normalized expansion $f(z) = z + \Sigma n = 2 \infty an(f)zn, z \in D, n=2$ and we impose on such functions f the second normalization $f(1) = \infty$. We call these functions concave schlicht functions, as the image of D is a concave domain. We prove that the sharp inequalities $|an(f)-n+1/2 \le n-1/2, n\ge 2$, are valid. This settles a conjecture formulated in [2]. © Swiss Mathematical Society.

Keywords

Concave schlicht functions, Slit mappings, Taylor coefficients