1. Introduction

In references [1-4] we have solved the problem of exact calculation of the field of refraction of a spherical electromagnetic wave on flat boundary of section of media with due account of the electrical and magnetic properties and also conductivity of real physical media by use of the updating of the mirror images method developed by us. At this, we have obtained the exact solutions for all spectrum of frequencies of the EM field. Now, we represent the results of application of this technique for the problems when the field is admissible to consider as stationary one [5], and we can assume, that $\omega \rightarrow 0$. At $\omega = 0$ the field of elementary electrical vibrator is defined by expressions (see [5] and Fig. 1):

$$H_\varphi = -\frac{I_3 l \sin \Theta}{4\pi r^2},$$  \hspace{1cm} (1)

$$E_r = \frac{I_3 l \cos \Theta}{\gamma_3 2\pi r^3},$$  \hspace{1cm} (2)

$$E_\Theta = \frac{I_3 l \sin \Theta}{\gamma_3 4\pi r^3}.$$  \hspace{1cm} (3)

Scalar potential and strength of an electric field of a charge have form:

$$\varphi = \frac{q}{4\pi \varepsilon_a r},$$  \hspace{1cm} (4)

$$E_r = \frac{q}{4\pi \varepsilon_a r^2}.$$  \hspace{1cm} (5)

For case shown in Fig. 1 the field is raised by a horizontally polarized wave/ Using the modified method of mirror images consider now geometry of calculated fields and currents.
2. Horizontally polarized field

For spherical horizontally polarized wave excited by the element of an alternating current (see Fig. 1) using the results of [1-3] we obtain the following dependences between currents:

\[
\dot{I}_{y2} = \frac{W_2 \cos \varphi - W_1 \cos \varphi_3}{W_2 \cos \varphi + W_1 \cos \varphi_3} \dot{I}_{y1},
\]

\[
\dot{I}_{y3} = \frac{2W_1 \cos \varphi}{W_2 \cos \varphi + W_1 \cos \varphi_3} \frac{\gamma_1^2}{\gamma_2^2} \dot{I}_{y1},
\]

and geometrical expressions:

\[
\frac{r_1}{r_3} = \frac{\gamma_2}{\gamma_1}, \quad \frac{\sin \varphi}{\sin \varphi_3} = \frac{\gamma_2}{\gamma_1}
\]

where

\[
W_1 = \sqrt{\frac{\mu_{a1}}{\varepsilon_{a1}}} \quad \text{and} \quad W_2 = \sqrt{\frac{\mu_{a2}}{\varepsilon_{a2}}}
\]

in expressions (6), (7) are the wave resistances of media.

At \( \omega = 0 \) these expressions take form
\[
I_{y2} = \frac{\sqrt{\mu_2} \cos \varphi - \sqrt{\mu_1} \cos \varphi_3}{\sqrt{\gamma_2} \cos + \sqrt{\gamma_1} \cos \varphi_3} I_{y1}, \quad (9)
\]

\[
I_{y3} = \frac{2 \sqrt{\mu_1} \cos \varphi}{\sqrt{\gamma_2} \cos + \sqrt{\gamma_1} \cos \varphi_3} \frac{\gamma_1 \mu_1 a_1}{\gamma_2 \mu_2 a_2} I_{y1}; \quad (10)
\]

\[
\frac{\eta_1}{r_3} = \frac{\gamma_2 \mu_2 a_2}{\gamma_1 \mu_1 a_1}, \quad \frac{\sin \varphi}{\sin \varphi_3} = \frac{\gamma_2 \mu_2 a_2}{\gamma_1 \mu_1 a_1}. \quad (11)
\]

The calculation algorithm is the following:
1) field of the element of current is calculated using expressions (1)-(5);
2) values of \( I_2, I_3, r_3 \) and \( \varphi_3 \) for all points on the boundary of section of media are defined using formulas (9)-(11);
3) field intensity in any point of space is calculated using extrapolation of a solution obtained for boundary of section of media following to procedure of a method of mirror images.

The pictures for electrical and magnetic fields obtained as a result of calculation are shown in Figs. 2 and 3.

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**Fig. 2. Electrical field |E|. Top to a floor-space – air. Current is at height 10 m.**

Current intensity \( I = 1 \text{A}, l = 0.1 \text{m} \).
3. Discussion of results and model of a thin conductor with a current with due account of a conductor material

It is necessary to pay attention to that, with direct using of procedure described, the strength of an electric field calculated is abnormally high (see Fig. 2). It is connected by that the equations for Hertz dipole were written for ideal calculation scheme. Let us analyze known formula [6]

\[ \dot{E} = \frac{1}{i\omega\varepsilon_a} \text{rot} \, \dot{H} . \]

It is obvious, that \( i\omega\varepsilon_a \dot{E} = \text{rot} \, \dot{H} \), that is identical

\[ j = \text{rot} \, \dot{H} \]

where \( j \) is the current density.
In case of when the current proceeds on a wire it is necessary to take parameters of a material of a wire, instead of environments. According to that, dependences (2) and (3) will take the form of

\[ \dot{E}_r = \frac{i\omega e^{-i\gamma r}}{i\omega\varepsilon_{an}} \frac{\cos \Theta}{2\pi r^3} \left(1 + i\gamma r \right) . \]
\[ E_\Theta = \frac{i \dot{E}_r e^{-i \gamma r} \sin \Theta}{i \omega \vec{\varepsilon}_{anp} 4\pi r^3} \left(1 + i \gamma r - \gamma^2 r^2 \right) \]

or

\[ E_r = \frac{\dot{E}_r e^{-i \gamma r} V \cos \Theta}{2\pi r^3} \left(1 + i \gamma r \right), \quad (12) \]

\[ E_\Theta = \frac{\dot{E}_r e^{-i \gamma r} V \sin \Theta}{4\pi r^3} \left(1 + i \gamma r - \gamma^2 r^2 \right) \quad (13) \]

where \( \dot{E}_r = \dot{U} \) is voltage; \( V \) is the conductor volume. At \( \omega = 0 \) we obtain

\[ E_r = \frac{E_\gamma V \cos \Theta}{2\pi r^3} = \frac{I_2 l \cos \Theta}{\gamma_{anp} 2\pi r^3}, \quad (14) \]

\[ E_\Theta = \frac{E_\gamma V \sin \Theta}{4\pi r^3} = \frac{I_2 l \sin \Theta}{\gamma_{anp} 4\pi r^3}, \quad (15) \]

that quite corresponds to classical representations.

Let us consider now how it will affect final dependences.

Dependences between electrical and magnetic components, and also between currents take form:

\[ \dot{W}_\Theta = \frac{\dot{E}_\Theta}{H_\phi} = -\frac{1 + i \gamma r - \gamma^2 r^2}{i \omega \vec{\varepsilon}_{anp} r (1 + i \gamma r)}. \]

\[ \dot{i}_{y2} = \frac{\gamma_2 \cos \phi - \gamma_1 \cos \phi_3}{\gamma_2 \cos \phi + \gamma_1 \cos \phi_3} \dot{i}_{y1}, \quad (16) \]

\[ \dot{i}_{y3} = \frac{2 \gamma_1 \cos \phi}{\gamma_2 \cos \phi + \gamma_1 \cos \phi_3} \frac{\gamma_1^2}{\gamma_2^2} \dot{i}_{y1}. \quad (17) \]

As consequence, dependences between currents for stationary electromagnetic field become following:

\[ i_{y2} = \frac{\sqrt{\gamma_2 \mu_2 a_2} \cos \phi - \sqrt{\gamma_3 \mu_1 a_1} \cos \phi_3}{\sqrt{\gamma_2 \mu_2 a_2} \cos \phi + \sqrt{\gamma_3 \mu_1 a_1} \cos \phi_3} i_{y1}, \]
\[ I_{y3} = \frac{2\sqrt{\gamma_2 \mu_{a1}} \cos \varphi}{\sqrt{\gamma_2 \mu_{a2}} \cos \varphi + \sqrt{\gamma_2 \mu_{a1}} \cos \varphi} \gamma_{21} \mu_{a1} I_{y1}. \]

The dependences between radius-vectors and angles will not change. As a result, instead of the pictures of fields represented in Figs. 2 and 3, we have obtained the results shown in Figs. 4 and 5.

**Fig. 4. Electrical field \(|E|\). Top to a floor-space – air. Bottom to a floor-space – the ground. Current is at height 10 m. Current intensity \( I_1 = 1 \text{A}, l = 0.1 \text{m} \).**

**Fig. 5. Magnetic field \(|H|\).**
4. Conclusions

In conclusion let us note the following.
1. At comparison of Figs. 2 and 4 it is evident, that strength of an electric field differs in $10^{20}$ times. It is explained that in the first case the current flows in a dielectric (air), and in the second case it flows in a conductor.
2. At the analysis of Figs. 3 and 5 it is visible, that character of a field corresponds to field calculated for a case when the segment of a wire is located above the ferromagnetic plane. In our case the plane is not ferromagnetic, but only spending. This effect is explained that in an offered method we consider not only magnetic properties of media, but also spending ones.
3. It is necessary to calculate the field of a conductor with alternating current under the formulas considering the material of conductor, namely: (1), (4), (5), (9), (10), fictitious currents under (16), (17) using geometrical expressions (8).

References