



ELSEVIER

Available online at www.sciencedirect.com

SCIENCE @ DIRECT®

LINEAR ALGEBRA
AND ITS
APPLICATIONS

Linear Algebra and its Applications 415 (2006) 210–229

www.elsevier.com/locate/laa

Preconditioned iterative methods for a class of nonlinear eigenvalue problems[☆]

Sergey I. Solov'ëv

*Faculty of Computer Science and Cybernetics, Kazan State University, Kremlevskaya 18,
420008 Kazan, Russian Federation*

Received 28 October 2004; accepted 14 March 2005

Available online 23 June 2005

Submitted by A. Knyazev

Abstract

This paper proposes new iterative methods for the efficient computation of the smallest eigenvalue of symmetric nonlinear matrix eigenvalue problems of large order with a monotone dependence on the spectral parameter. Monotone nonlinear eigenvalue problems for differential equations have important applications in mechanics and physics. The discretization of these eigenvalue problems leads to nonlinear eigenvalue problems with very large sparse ill-conditioned matrices monotonically depending on the spectral parameter. To compute the smallest eigenvalue of large-scale matrix nonlinear eigenvalue problems, we suggest preconditioned iterative methods: preconditioned simple iteration method, preconditioned steepest descent method, and preconditioned conjugate gradient method. These methods use only matrix–vector multiplications, preconditioner–vector multiplications, linear operations with vectors, and inner products of vectors. We investigate the convergence and derive grid-independent error estimates for these methods. Numerical experiments demonstrate the practical effectiveness of the proposed methods for a model problem.

© 2005 Elsevier Inc. All rights reserved.

[☆] The work of the author was performed while visiting Technische Universität Chemnitz. This work was supported by Alexander von Humboldt–Stiftung (Alexander von Humboldt Foundation) and Deutsche Forschungsgemeinschaft (German Research Foundation), Sonderforschungsbereich (Collaborative Research Center) 393.

E-mail address: sergei.solovyev@ksu.ru