

Inflation in an effective gravitational model and asymptotic safety

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Abstract

© 2018 American Physical Society. We consider an inflationary model motivated by quantum effects of gravitational and matter fields near the Planck scale. Our Lagrangian is a resummed version of the effective Lagrangian recently obtained by Demmel, Saueressig, and Zanusso [A proper fixed functional for four-dimensional quantum Einstein gravity, J. High Energy Phys. 08 (2015) 113. JHEPFG1029-8479 10.1007/JHEP08(2015)113] in the context of gravity as an asymptotically safe theory. It represents a refined Starobinsky model, $\mathcal{L}_{\text{eff}} = M^2 R/2 + (a/2) R^2/[1 + b \ln(R/\mu^2)]$, where R is the Ricci scalar, a and b are constants, and μ is an energy scale. By implementing the COBE normalization and the Planck constraint on the scalar spectrum, we show that increasing b leads to an increased value of both the scalar spectral index n_s and the tensor-to-scalar ratio r . Requiring n_s to be consistent with the Planck Collaboration upper limit, we find that r can be as large as $r \approx 0.01$, the value possibly measurable by Stage IV CMB ground experiments and certainly from future dedicated space missions. The predicted running of the scalar spectral index $\alpha = dn_s/d \ln(k)$ is still of the order -5×10^{-4} (as in the Starobinsky model), about 1 order of magnitude smaller than the current observational bound.

<http://dx.doi.org/10.1103/PhysRevD.98.043505>

References

- [1] A. A. Starobinsky, Spectrum of relict gravitational radiation and the early state of the universe, *Pis'ma Zh. Eksp. Teor. Fiz.* 30, 719 (1979) PZETAB 0370-274X
- [2] [A. A. Starobinsky *JETP Lett.* 30, 682 (1979)]. JPLA2 0021-3640
- [3] A. A. Starobinsky, A new type of isotropic cosmological models without singularity, *Phys. Lett. B* 91, 99 (1980). PYLBAJ 0370-2693 10.1016/0370-2693(80)90670-X
- [4] A. H. Guth, The inflationary universe: A possible solution to the horizon and flatness problems, *Phys. Rev. D* 23, 347 (1981). PRVDAQ 0556-2821 10.1103/PhysRevD.23.347
- [5] A. D. Linde, A new inflationary universe scenario: A possible solution of the horizon, flatness, homogeneity, isotropy and primordial monopole problems, *Phys. Lett. B* 108, 389 (1982). PYLBAJ 0370-2693 10.1016/0370-2693(82)91219-9
- [6] J. F. Donoghue, General relativity as an effective field theory: The leading quantum corrections, *Phys. Rev. D* 50, 3874 (1994). PRVDAQ 0556-2821 10.1103/PhysRevD.50.3874
- [7] P. A. R. Ade (Planck Collaboration), Planck 2015 results. XX. Constraints on inflation, *Astron. Astrophys.* 594, A20 (2016). AAEJAF 0004-6361 10.1051/0004-6361/201525898
- [8] A. A. Starobinsky, Nonsingular model of the Universe with the quantum-gravitational de Sitter stage and its observational consequences, in *Proceedings of the Second Seminar, Quantum Theory of Gravity (Moscow, 1981)* (INR Press, Moscow, 1982), p. 58;

- [9] reprinted in Quantum Gravity, edited by M. A. Markov and P. C. West (Plenum, New York, 1984), p. 103.
- [10] K. P. Stanyukovich, Gravitational Field and Elementary Particles [(Gravitatsionnoie pole i elementarnyie chastitsy) (Nauka, Moscow, 1965).
- [11] B. S. DeWitt, Quantum theory of gravity. 1. The canonical theory, Phys. Rev. 160, 1113 (1967). PHRVAO 0031-899X 10.1103/PhysRev.160.1113
- [12] B. S. DeWitt, Quantum theory of gravity. 3. Applications of the covariant theory, Phys. Rev. 162, 1239 (1967). PHRVAO 0031-899X 10.1103/PhysRev.162.1239
- [13] V. L. Ginzburg, D. A. Kirzhnits, and A. A. Lyubushin, The role of quantum fluctuations of the gravitational field in general relativity and cosmology, Zh. Eksp. Teor. Fiz. 60, 451 (1971) ZETFA7 0044-4510
- [14] [V. L. Ginzburg, D. A. Kirzhnits, and A. A. Lyubushin Sov. Phys. JETP 33, 242 (1971)]. SPHJAR 0038-5646
- [15] Ya. B. Zeldovich and A. A. Starobinsky, Particle production and vacuum polarization in an anisotropic gravitational field, Zh. Eksp. Teor. Fiz. 61, 2161 (1971) ZETFA7 0044-4510
- [16] [Ya. B. Zeldovich and A. A. Starobinsky Sov. Phys. JETP 34, 1159 (1972)]. SPHJAR 0038-5646
- [17] G. 't Hooft and M. J. G. Veltman, One loop divergences in the theory of gravitation, Ann. Inst. Henri Poincaré, A 20, 69 (1974).
- [18] M. H. Goroff and A. Sagnotti, Quantum gravity at two loops, Phys. Lett. B 160, 81 (1985). PYLBAJ 0370-2693 10.1016/0370-2693(85)91470-4
- [19] A. E. M. van de Ven, Two loop quantum gravity, Nucl. Phys. B378, 309 (1992). NUPBBO 0550-3213 10.1016/0550-3213(92)90011-Y
- [20] S. Weinberg, Critical Phenomena for Field Theorists (Springer, New York, 1979).
- [21] S. Weinberg, in General Relativity: An Einstein Centenary Survey, edited by S. W Hawking and W. Israel (Cambridge University Press, Cambridge, England, 1979), p. 790.
- [22] S. Weinberg, Effective field theory, past and future, Int. J. Mod. Phys. A 31, 1630007 (2016). IMPAEF 0217-751X 10.1142/S0217751X16300076
- [23] S. Weinberg, Effective field theory, past and future, Proc. Sci., CD09 (2009) 001, arXiv:0908.1964.
- [24] M. Reuter, Nonperturbative evolution equation for quantum gravity, Phys. Rev. D 57, 971 (1998). PRVDAQ 0556-2821 10.1103/PhysRevD.57.971
- [25] M. Reuter and F. Saueressig, Quantum Einstein gravity, New J. Phys. 14, 055022 (2012). NJOPFM 1367-2630 10.1088/1367-2630/14/5/055022
- [26] M. Demmel, F. Saueressig, and O. Zanusso, A proper fixed functional for four-dimensional quantum Einstein gravity, J. High Energy Phys. 08 (2015) 113. JHEPFG 1029-8479 10.1007/JHEP08(2015)113
- [27] C. Fang and Q. G. Huang, The trouble with asymptotically safe inflation, Eur. Phys. J. C 73, 2401 (2013). EPCFFB 1434-6044 10.1140/epjc/s10052-013-2401-2
- [28] Q.-G. Huang, A polynomial $f(R)$ inflation model, J. Cosmol. Astropart. Phys. 02 (2014) 035. JCAPBP 1475-7516 10.1088/1475-7516/2014/02/035
- [29] A. Marunović and T. Prokopec, Planck scale operators, inflation and fine tuning, Phys. Rev. D 96, 043512 (2017). PRVDAQ 2470-0010 10.1103/PhysRevD.96.043512
- [30] M. Reuter and F. Saueressig, From big bang to asymptotic de Sitter: Complete cosmologies in a quantum gravity framework, J. Cosmol. Astropart. Phys. 09 (2005) 012. JCAPBP 1475-7516 10.1088/1475-7516/2005/09/012
- [31] A. Bonanno and M. Reuter, Cosmology of the Planck era from a renormalization group for quantum gravity, Phys. Rev. D 65, 043508 (2002). PRVDAQ 0556-2821 10.1103/PhysRevD.65.043508
- [32] A. Bonanno and M. Reuter, Cosmology with self-adjusting vacuum energy density from a renormalization group fixed point, Phys. Lett. B 527, 9 (2002). PYLBAJ 0370-2693 10.1016/S0370-2693(01)01522-2
- [33] A. Bonanno, A. Contillo, and R. Percacci, Inflationary solutions in asymptotically safe $f(R)$ theories, Classical Quantum Gravity 28, 145026 (2011). CQGRDG 0264-9381 10.1088/0264-9381/28/14/145026
- [34] K. Falls, D. F. Litim, K. Nikolakopoulos, and C. Rahmede, On de Sitter solutions in asymptotically safe (Equation presented) theories, Classical Quantum Gravity 35, 135006 (2018). CQGRDG 0264-9381 10.1088/1361-6382/aac440
- [35] S. Weinberg, Asymptotically safe inflation, Phys. Rev. D 81, 083535 (2010). PRVDAQ 1550-7998 10.1103/PhysRevD.81.083535
- [36] S.-H. H. Tye and J. Xu, Comment on asymptotically safe inflation, Phys. Rev. D 82, 127302 (2010). PRVDAQ 1550-7998 10.1103/PhysRevD.82.127302
- [37] M. Hindmarsh, D. Litim, and C. Rahmede, Asymptotically safe cosmology, J. Cosmol. Astropart. Phys. 07 (2011) 019. JCAPBP 1475-7516 10.1088/1475-7516/2011/07/019
- [38] A. Bonanno and F. Saueressig, Asymptotically safe cosmology-A status report, C.R. Phys. 18, 254 (2017). CRPOBN 1631-0705 10.1016/j.crhy.2017.02.002

- [39] Y. F. Cai and D. A. Easson, Asymptotically safe gravity as a scalar-tensor theory and its cosmological implications, *Phys. Rev. D* 84, 103502 (2011). PRVDAQ 1550-7998 10.1103/PhysRevD.84.103502
- [40] E. J. Copeland, C. Rahmede, and I. D. Saltas, Asymptotically safe Starobinsky inflation, *Phys. Rev. D* 91, 103530 (2015). PRVDAQ 1550-7998 10.1103/PhysRevD.91.103530
- [41] A. Codello, J. Joergensen, F. Sannino, and O. Svendsen, Marginally deformed Starobinsky gravity, *J. High Energy Phys.* 02 (2015) 50. JHEPFG 1029-8479 10.1007/JHEP02(2015)050
- [42] K. Bamba, G. Cognola, S. D. Odintsov, and S. Zerbini, One-loop modified gravity in a de Sitter universe, quantum-corrected inflation, and its confrontation with the Planck result, *Phys. Rev. D* 90, 023525 (2014). PRVDAQ 1550-7998 10.1103/PhysRevD.90.023525
- [43] I. Ben-Dayan, S. Jing, M. Torabian, A. Westfal, and L. Zarate, (Equation presented) quantum corrections and the inflationary observables, *J. Cosmol. Astropart. Phys.* 09 (2014) 005. JCAPBP 1475-7516 10.1088/1475-7516/2014/09/005
- [44] A. Bonanno and A. Platania, Asymptotically safe inflation from quadratic gravity, *Phys. Lett. B* 750, 638 (2015). PYLBAJ 0370-2693 10.1016/j.physletb.2015.10.005
- [45] M. Rinaldi, G. Cognola, L. Vanzo, and S. Zerbini, Reconstructing the inflationary (Equation presented) from observations, *J. Cosmol. Astropart. Phys.* 08 (2014) 015. JCAPBP 1475-7516 10.1088/1475-7516/2014/08/015
- [46] S. R. Coleman and E. J. Weinberg, Radiative corrections as the origin of spontaneous symmetry breaking, *Phys. Rev. D* 7, 1888 (1973). PRVDAQ 0556-2821 10.1103/PhysRevD.7.1888
- [47] N. Alkofer and F. Saueressig, Asymptotically safe (Equation presented)-gravity coupled to matter I: the polynomial case, arXiv:1802.00498.
- [48] V. T. Gurovich and A. A. Starobinsky, Quantum effects and regular cosmological models, *Sov. Phys. JETP* 50, 844 (1979). SPHJAR 0038-5646
- [49] G. K. Chakravarti and S. Mohanty, Power law Starobinsky model of inflation from no-scale SUGRA, *Phys. Lett. B* 746, 242 (2015). PYLBAJ 0370-2693 10.1016/j.physletb.2015.04.056
- [50] H. Motohashi, Consistency relation for (Equation presented) inflation, *Phys. Rev. D* 91, 064016 (2015). PRVDAQ 1550-7998 10.1103/PhysRevD.91.064016
- [51] L. H. Liu, Analysis of (Equation presented) inflationary model as (Equation presented), arXiv:1807.00666.
- [52] M. Rinaldi, G. Cognola, L. Vanzo, and S. Zerbini, Inflation in scale-invariant theories of gravity, *Phys. Rev. D* 91, 123527 (2015). PRVDAQ 1550-7998 10.1103/PhysRevD.91.123527
- [53] N. Palanque-Delabrouille, Cosmology with Lyman-alpha forest power spectrum, *J. Cosmol. Astropart. Phys.* 11 (2015) 011. JCAPBP 1475-7516 10.1088/1475-7516/2015/11/011
- [54] P. A. R. Ade (BICEP2 and Planck Collaborations), Joint Analysis of (Equation presented) and Planck Data, *Phys. Rev. Lett.* 114, 101301 (2015). PRLTAO 0031-9007 10.1103/PhysRevLett.114.101301
- [55] P. A. R. Ade (BICEP2 and Keck Array Collaborations), Improved Constraints on Cosmology and Foregrounds from BICEP2 and Keck Array Cosmic Microwave Background Data with Inclusion of 95 GHz Band, *Phys. Rev. Lett.* 116, 031302 (2016). PRLTAO 0031-9007 10.1103/PhysRevLett.116.031302
- [56] Y. Akrami (Planck Collaboration), Planck 2018 results. X. Constraints on inflation, arXiv:1807.06211.
- [57] F. R. Bouchet (CORÉ Collaboration), CORÉ (Cosmic Origins Explorer) A White Paper, arXiv:1102.2181.
- [58] T. Matsumura, Mission design of LiteBIRD, *J. Low Temp. Phys.* 176, 733 (2014). JLTAPAC 0022-2291 10.1007/s10909-013-0996-1
- [59] S. A. Appleby, R. A. Battye, and A. A. Starobinsky, Curing singularities in cosmological evolution of (Equation presented) gravity, *J. Cosmol. Astropart. Phys.* 06 (2010) 005. JCAPBP 1475-7516 10.1088/1475-7516/2010/06/005
- [60] A. A. Starobinsky, Dynamics of phase transition in the new inflationary Universe scenario and generation of perturbations, *Phys. Lett. B* 117, 175 (1982). PYLBAJ 0370-2693 10.1016/0370-2693(82)90541-X
- [61] A. A. Starobinsky, The perturbation spectrum evolving from a nonsingular, initially de Sitter cosmology, and the microwave background anisotropy, *Pisma v Astron. Zh.* 9, 579 (1983) SALEDW 0360-0327
- [62] [A. A. Starobinsky *Sov. Astron. Lett.* 9, 302 (1983)].
- [63] L. A. Kofman and V. F. Mukhanov, Evolution of perturbations in an inflationary universe, *Pis'ma Zh. Eksp. Teor. Fiz.* 44, 481 (1986) PZETAB 0370-274X
- [64] [L. A. Kofman and V. F. Mukhanov *JETP Lett.* 44, 619 (1986)]. JTPLA2 0021-3640
- [65] V. F. Mukhanov and G. V. Chibisov, Quantum fluctuations and a non-singular universe, *Pis'ma Zh. Eksp. Teor. Fiz.* 33, 549 (1981) PZETAB 0370-274X
- [66] [V. F. Mukhanov and G. V. Chibisov *JETP Lett.* 33, 532 (1981)]. JTPLA2 0021-3640
- [67] J.-C. Hwang and H. Noh, Cosmological perturbations in generalized gravity theories, *Phys. Rev. D* 54, 1460 (1996). PRVDAQ 0556-2821 10.1103/PhysRevD.54.1460