

# Effects of modified gravity on the turnaround radius in cosmology

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## Abstract

© 2018 American Physical Society. We revisit the concept of turnaround radius in cosmology, in the context of modified gravity. While preliminary analyses were limited to scalar-tensor/F(R) gravity, we extend the definition and the study of this quantity to a much broader class of theories including also quantum R<sup>2</sup> gravity. The turnaround radius is computed in terms of the parameters of the theory, and it is shown that a deviation not larger than 10% of this quantity from its value in Einstein's theory could constrain the model parameters and even rule out some current theories.

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